StructureandPerformanceEvaluationofa ReplicatedBanyanNetworkBasedATMSwitch

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Abstract

Banyannetworksarecommonlyusedas interconnectionstructures in ATM switches. This paper is concernedwiththereplicationtechniquewhichwas appliedtothestandardbanyannetworks.Inthispaper, weapplythistechniquetothePlaneInterconnected ParallelNetwork(PIPN)whichisaswitchintroduced previouslyasabetterbanyanbasedinterconnection structure. The normalized throughput of unbuffered and bufferedreplicatedPI PNisanalyzedanalyticallyunder uniformtrafficmodel. Weapplythesimulation technique toverifytheanalyticalresultsundertheuniformtraffic modelandtostudytheperformanceofdifferent heterogeneoustrafficmodels. The performance is shown to increase significantly when the replicated PIPN is used whichsupports the idea of using this switch as a new high performanceATMswitch.

IndexTerms –*ATMswitching,banyannetworks, replicatednetworks.*

1.Introduction

Duetothehightransmissionca pacityofferedbyfiber optics,manyapplicationsthatrequirehighbandwidth haveemerged[1].Thecreationofanetworkthatprovides highbandwidthservicestotheusersisneeded.The challengeistobuildlargeswitchesthatcanoperateatthe highdatatransferratesandmeettheperformance requirements.

Banyannetworksarecommonlyusedinmultistage ATMswitchesbecauseoftheirhighdegreeofparallelism, self-routing,modularity,constantdelayforallinput outputportpairs,in -orderdelivery ofcells,andsuitability forVLSIimplementation[2 -8].However,inbanyan networks,thereisonlyonepathbetweeneachinputand outputportpair,andtheedgesofsuchapatharenot dedicated.Thismeansthatothercommunicatingpairs maysharesomelinksofapathconnectinganinput -output portpair. The concernof this paper is to design an ewhigh performance ATMs witch. The switch combine the technique of replication with the plane interconnected parallel network (PIPN). The replication technique was applied on the bany annetworks to enhance their performance [2,3]. PIPN was introduced in [4] as a better bany an based interconnection structure. By combining the two techniques, we take the advantage of replication which provides multiple paths from each input to each output, thus decreasing the effect of conflict between cells, and the advantage of PIPN which gives better performance under heterogeneous traffic over the standard bany annetwork.

Theoutlineofthispaperisasfollows:Insection2, describethebasicstructureandoperationofthe ReplicatedPIPNswitch.Insection3,wediscussits performanceunderuniformandheterogeneoustraffic models.Weconcludethepaperinsection4.

2. Thereplicated PIPNs witch

2.1.Background

AcellswitchisaboxwithNinputsandNoutputs whichroutesthecellsarrivingatitsinputstotheir requestedoutputs. The general cells witch architecture is showninFig.1.Severalarchitecturaldesignshave emergedtoimplementthisswitch. They may b eclassified intothreecategories:theshared -memorytype,theshared mediumtype,andthespace -divisiontype.Bothshared memoryandshared -mediumsufferfromtheirstrict capacitylimitation,whichislimitedtothecapacityofthe internal communication medium. Any internal link is N timesfasterthantheinputlinkanditisusually implementedasaparallelbus.Thismakessuch architecturesmoredifficulttoimplementasNbecomes large.Fig.2showstheshared -mediumandshared memoryarchitecture s.





Fig.2.Sharedmediumandsharedmemory architectures

Thesimplestspace -divisionswitchisthecrossbar switch, which consists of as quarearray of NxN crosspointswitches.oneforeachinput -outputpairas showninFig.3.Aslongasthereisnooutputconflicts,all incomingcellscanreachtheirdestinations. If, on the other hand, there is more than one cell destined in the same time slottothesameoutput, the nonlyone of the secells can be routedandtheothercellsmaybedroppedorbuffered. Themajordrawbackofthecrossbarswitchs temsfromthe ²crosspoints, and therefore, the factthatitcomprisesN sizeofrealizablesuchswitchesislimited.Forthisreason, alternativecandidatesforspacedivisionswitchingfabrics havebeen introduced. These alternatives are based on a classofmultistageinterconnectionnetworkscalled banyannetworks[1].



Fig.3.Crossbararchitecture

Abanyannetworkconstructedfrom2x2switching elements(SE)consistsofn=log 2Nstages(Nisassumed tobeapowerof2).Banyannetworkshavemanydesirable properties:highdegre eofparallelism,self -routing, modularity,constantdelayforallinput -outputportpairs, in-orderdeliveryofcells,andsuitabilityforVLSI implementation.Theirshortcomingremainsblockingand throughputlimitation.Blockingoccurseverytimetwo cellsarriveataswitchingelementandrequestthesame outputlinkoftheswitchingelement.Theexistenceof suchconflicts(whichmayariseevenifthetwocellsare destinedtodistinctoutputports)leadstoamaximum achievablethroughputwhichismuc hlowerthanthat obtainedwiththecrossbarswitch.An8x8banyannetwork isshowninFig.4.



Fig.4.Abanyannetwork

Toovercometheperformancelimitationsofbanyan networks,variousperformanceenhancingtechniqueshave beenintroduced[2,3,6,7].Thesetechniqueshavebeen widelyusedindesigningATMswitches[2 -8].

Oneoftheperformanceenhancementtechniquesof banyannetworksisthereplicationtechnique[2,3].Using thereplicationtechnique, we have R=2 r(r=1,2,...)parallelsubnetwo rks.Eachofthesesubnetworksisa banyannetwork.Twotechniquesareusedtodistributethe incomingcellsovertheRsubnetworks.Inthefirst technique.inputioftheswitchisconnectedtoinputiof eachsubnetbya1 -to-Rdemultiplexer.Thedemultiplexer forwardstheincomingcellsrandomlyacrossthe subnetworks.Similarly,eachoutputiofasubnetis connected to the output iof the switch through a R -to-1 multiplexer.Ifmorethanonecellarriveatthe multiplexer, one of the misselected rand omlytobe forwardedtotheoutputportandtheothersarediscarded. Thistechniqueiscalledrandomlyloadingparallel networks(Rn)[2,3].Fig.5showsa4x4randomlyloaded banyannetworkconstructedfromtwo4x4banyan networks.

Thesecondtechniquegroupstheoutputsoftheswitch andassignseachgrouptooneofRtruncatedsubnetworks. Thei thinputoftheswitchisconnectedtothei thinputof eachsubnetthroughal -to-Rdemultiplexer.The demultiplexerforwardsincomingcellsaccordingtotheir mostsignificantbitsofthedestinationaddressfield.Each truncatedsubnethasn -rstages.Theoutputsofeach subnetwhicharedestinedtothesameswitchoutputare connectedviaaR -to-1multiplexertothisoutput.This techniqueiscalledselectivelyloadingparallelnetworks (Sn)[2].A4x4selectivelyloadedparallelbanyannetwork constructedfromtwo4x4truncatedbanyannetworksis showninFig.6.







Fig.6.A4x4selectivelyloadedbanyannetwork constructedformtwo4x4truncatedbanyannetworks

Theperformanceofbanyanbasedsw itchesdependson theappliedtraffic.Astheappliedtrafficbecomes heterogeneous,theperformanceofbanyanbasedswitches degradedrasticallyevenifsomeperformanceenhancing techniquesareemployed.

In[4],thePIPN,anewbanyanbasedinterconnection structurewhichexploitsthedesiredpropertiesofbanyan networkswhileimprovingtheperformancebyalleviating theirdrawbacks,isintroduced.InPIPN,thetraffic arrivingatthenetworkisshapedandroutedthroughtwo banyannetworkbasedintercon nectedplanes.The interconnectionbetweentheplanesdistributesthe incomingloadmorehomogeneouslyoverthenetwork.

PIPNiscomposed of three main units, namely, the distributor, the router, and the output -portdispatcheras showninFig.7[4,5].Thecellsarrivingatthedistributor dividesthenetworkintotwogroupsinarandommanner: thebackplaneandthefrontplanegroups. The destination address fields of cells in one of the groups arecomplemented.Thegroupedcellsareassignedtothe router,whichisaN/2xN/2banyannetwork.Thecellsare routedwithrespecttotheinformationkeptintheir destinationaddressfields.Duetotheinternalstructureof therouterandthemodificationsinthedestinationaddress fields of some cells, an outlet of the router may have cells actually destined to four different output ports. The cells arriving from the outlets of the router are assigned to therequestedoutputportsintheoutput -portdispatcher[4,5]. Theoutput -portdispatcherhastwodiffer entsub -units:the deciderandthecollector.Thereisadeciderunitforeach routeroutputandacollectorunitforeachoutputport. ThereareatotalofNdecidersandNcollectors.The deciderdeterminestowhichoutputportanarrivingcell willbeforwardedandrestoresitsdestinationaddress field.Eachcollectorhasfourinletsandinternalbufferto accommodatethecellsarrivingfromfourpossible deciders.

2.2. Thereplicated PIPNs witch structure

TheReplicatedPIPNswitchappliesthereplic ation techniquetothePIPNtobenefitfromtheadvantageof bothtechniques.Replicationprovidesmultiplepathsfrom eachinputtoeachoutputpair,thusdecreasingtheeffect ofconflictbetweencells.PIPNgivesbetterperformance underheterogeneoustrafficoverthestandardbanyan network.

A8x8RandomlyLoadedPIPNforR=2isshownin Fig.8.ItisshownfromthefigurethattheReplicated PIPNiscomposedofRPIPN'sconnectedinparallel.No multiplexersareneededattheoutputoftherouterasth decidersforwardtheincomingcellstothecollectors' buffers.ThestructureoftheSelectivelyLoadedPIPNis similartothestructureoftheRandomlyLoadedPIPNbut theroutersaretruncated(haven -r-1stagesinsteadofn 1),andthedemultiplexerforwardcellstosubnetworks accordingtotheirrmostsignificantbitsoutputs.

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3.Performanceevaluationofthereplicated PIPNswitch

Inthissection, the throughput of the Replicated PIPN switchise valuated. Analytical analysis is performed under uniform traffic model. For simulation, a Timed Colored PetriNet [9] is used to model the original and the



ReplicatedPIPN.APetriNetmodelforan4x4banyan networkisgiveninFig.9.Itisshownfromthefigurethat thestructureofthePetriNetmodelisthesameasthatof theswitcheswitheachSEmodeledasshowninfigure.

3.1. ReplicatedPIPNperformanceunderthe uniformtrafficmodel

Inthissection, we study the performance of the Replicated PIPNs witch under uniform traffic model. In this model, cells are equiprobably destined to any output port. Thus, the load at the outlets of all SE's in the same stage will be the same.

Thethroughputofbanyannetworks, under uniform traffic model, was given in [2,3,5]. The performance of the original PIPN with sufficiently large buffer was studied in [4,5]. The performance of Replicated banyan

networks, both randomly and selectively loaded, was studied in [2,3].



Fig.9.APetriNetmodelfora4x4banyannetwork

Inthefollowin gsubsections,weperformbuffer dimensioninganalysisfortheoriginalPIPNandstudythe performanceoftheunbufferedandbufferedReplicated PIPN.

3.1.1.UnbufferedPIPN. ThethroughputofanNxN PIPNisachievedbyanN/2xN/2banyannetwork.This resultisdirectlyrelatedtothenumberofstagessincethe trafficisuniform.InanNxNbanyannetwork,therearen stages,however,inanNxNPIPNtherearen -1stagesin therouter[4,5].ThethroughputoftheoriginalPIPNwith sufficientlyla rgebufferwasstudiedin[4,5]andwas givenby:

$$X_{\text{banyan}} = 1 - \left(1 - \frac{X_{\text{PIPN}}}{2}\right)^2 \tag{1}$$

(forn etworksof thesame size)

wherethethroughputofabanyannetworkatstageiis givenin[2,3,5]by:

$$X_i = 1 - \left(1 - \frac{X_{i-1}}{2}\right)^2$$
 for $1 \le i \le n(2)$

ThethroughputofanNxNunbufferedPIPNunder uniformtrafficcanbefoundasfollows:

$$X_{\text{unbufferedPIPN}} = 1 - (1 - X_{\text{c}})^{4}$$
$$= 1 - \left(1 - \frac{X_{\text{banyanof sizeN/2xN/2}}}{4}\right)^{4} (3)$$

where $X_{banyanofsizeN/2xN/2}$ is the throughput of a banyan network with n -1 stages.

Fig.10showsthesimulationresultfortheoriginal PIPNunderuniformtrafficmodelforvariousbuffersizes. Thesimulationandanalyticalresultsareconsis tentfor buffersizeequalzero.Itisshownfromthefigurethata buffersizeoftwopereachcollectorissufficientto achieveperformancenearinfinitebuffer.Thusthisbuffer sizeischosenfortestingtheperformanceofReplicated PIPNswitchunderheterogeneoustraffictypes.

Inthefollowingsubsections, Xwilldenote the probability of finding acellatevery input of the switch at each slottime. The probability of finding acellate ach input of a subnet at each times lot is $X_{in} = X/R$.



Fig.10.EffectofbuffersizeonPIPN performance atfull load

3.1.2.UnbufferedreplicatedPIPNswitch. The performanceofanNxNunbufferedReplicatedPIPN switchwithreplicationdegree=Risstudiedinthis section.Westudytheperformanceofbothrandomlyand selectivelyloadedPIPN.Theperformanceofrandomly loadedbanyannetworkswasstudiedin[2]and[3]and wasgivenby:

$$X_{out} = 1 - (1 - x_n)^R$$
 (4)

where x_n is the throughput of a bany annetwork having n stages with a rrival rate equals X_{in} .

Theperformanceofselectivel yloadedbanyan networkswasstudiedin[2]andwasgivenby:

$$X_{out} = 1 - (1 - x_{n-r})^R$$
 (5)

wherexn -risthethroughputofabanyannetworkhaving n-rstageswitharrivalrateequalsXin.

A. UnbufferedrandomlyloadedPIPNswitch. Since the routerofeach subnet of the randomlyloaded PIPNswitch consists of n -1 stages, the output rate ach router's

$$X_{unbufferedrandomly loadedPIPN} = 1 - (1 - X_c)^{4.R}$$

 $\therefore X_{unbuffered randomly\ loaded PIP\ N}$

$$= 1 - \left(1 - \frac{X_{\text{banyanwit hn -1stagesa ndload} = X_{\text{in}}}{4}\right)^{4.R}$$
$$= 1 - \left(1 - X_{\text{unbufferedPIPN}}\right)^{R}$$
(6)

 $where X \quad {}_{unbuffered} PIPN is the throughput of an NxN unbuffered PIPN with load equal X in.$

Fig.11.ashowsthethroughputoftheunbuffered RandomlyLoadedPIPNswitchbothanalyticallyandby simulation.









X_{unbufferedselective lyloaded PIPN}

$$= 1 - \left(1 - \frac{X_{\text{banyanwit hn -r-1stages}}}{4}\right)^{4.R}$$
$$= 1 - (1 - X_{\text{unbufferedPIPN}})^{R} \qquad (7)$$

where $X_{unbufferedPIPN}$ is the throughput of a N/RxN/R unbuffered PIPN with load equal X_{in} .

Fig.11.bshowsthethroughputoftheunbuffered SelectivelyLoadedPIPNswitchboth analyticallyandby simulation.

3.1.3.BufferedreplicatedPIPNswitch. Since there are nolossofcells, the throughput of the randomly loaded Replicated PIPNswitch under infinite buffer is exactly R times the through put of a NxNPIPN with infinite buffer, given in equation (1).

 $X_{Randomlyl oaded PIPN withinfi nitebuffe r}$

$$R. X_{NxNPIPNw ithinfini tebuffer}$$
 (8)

Similarly, the throughput of these lectively loaded Replicated PIPNs witch under infinite buffer is exactly R times the through put of a N/RxN/RPIPN with infinite buffer, given in equation (1).

X_{SelectivelyloadedP} IPNwithi nfinitebu ffer

$$= R. X_{N/RxN/RPIPNwit hinfinite buffer}$$
(9)

Fig.11showsthethroughputoftheRandomlyand SelectivelyLoadedPIPNswitchwithinfinitebufferboth analyticallyandbysimulation.Itisshownfromthefigure thatthesimulationcurvedepartsfromtheanalyticalcurve fortheinfinitebuffercaseespeciallyforlargenetwork sizes.Theinfinitenumberofcellsinthebuffersjustifies thisdifferenceasalargenumberofcellsremaininthe bufferwaitingtobetransmitted.Thiseffectincreasesas thenetworksizeandreplication degreeincrease.





 $\label{eq:2} AlsoshowninFig.12thethroughputofR 2, R 4, S 2, and S 4 Replicated PIPNs witches with buffersize equal two cells percollector compared to the original PIPN with infinite buffer. It is shown from the figure that the throughput of these lectively loaded PIPN is better than$

that of the randomly loaded PIPN. This is expected as the former has fewer stages than the later.

3.2.ReplicatedPIPNperformanceunderType -I trafficmodel

InType -Itraffic,output portsaregrouped.Thenumber of groups is an integer power of two. The ports in the samegrouphaveanequalchanceofbeingselectedbyany incomingcell.However,eachgroupmayhaveadifferent selectionprobability. The parameters for the traffic type areselectedtocreateheterogeneousoutletrequests. The numberofparametersisselectedaseightsinceeightisa reasonablevalueforthenumberofoutletgroupsinthe range16 -256outlets[4,5].InFig.13,thenormalized throughputform=(0.3,0 .02,0.15,0.00,0.20,0.06,0.22, 0.05)Type -Itraffic with respect to varying incoming load anddifferentnetworksizesisshownfortheR 2,R 4,S 2, andS₄ReplicatedPIPNswitches,andtheoriginalPIPN. Thepercentagethroughputimprovementobtainedbythe ReplicatedPIPNisshowninTable1.

Itisshownfromthefigurethatthedifferencebetween theR 2, andR 4 curves increases as the switch size increase. This is expected as when the switch size increases, the number of stages increases resulting in contention. R 4 provides more paths for the cells than R 2. The same reason applies to S 2 and S 4.

3.3.ReplicatedPIPNperformanceunderType -II trafficmodel

InType -IItraffic,theinletsandtheoutletsareboth dividedintogroups.Althoughthesizeofinputgroupsis fixed,theoutputgroupshavedifferentsizes.Moreover, theselectionprobabilityofanoutputportgroupvaries dependingontheinputportnumberthatsendsthecell[4, 5,10].

Asprovedin[10], Type -II traffic represented by more than $\lceil \log_4 N \rceil + 1$ parameters on a bany annetwork can be represented by using $\lceil \log_4 N \rceil + 1$ parameters only. Therefore, there is no need to test the performance of the Replicated PIPN under Type -II traffic represented by more than $\lceil \log_4 N \rceil + 1$ parameters.

ThethroughputoftheR 2,R 4,S 2,andS 4Replicated PIPNandoriginalPIPNswitchesofsize256x256is evaluatedunder19patternsofType -IItrafficrepresented byfourparameterswithincomingload1.0.Thetraffic patternsarevariedbetweenuniformtra fficandthe extremeheterogeneouscasewhichispossibleunderthe giventraffictypeandparameters.Theaimistopresent thebehaviorofboththeReplicatedPIPNandtheoriginal PIPNundervarioustrafficpatterns.Thethroughputforall Type-IItrafficpatternsareshowninTable3inappendix A. TheobtainedresultsaresummarizedinTable2.The tableshowsthemaximum,minimum,averagethroughput values,andthestandarddeviationofeachnetworktype underthegiventrafficset.Itisshownfromt histablethat theReplicatedPIPNissuperiorovertheoriginalPIPN. WhenthereplicationtechniqueisappliedtoPIPN,it giveshighaveragethroughput.However,therandomly loadingtechniquegivesthesmallestthroughputrange (Max. –Min.).Thissmallthroughputrangeisagood indicationfortheconsistencyoftheswitchingsystemas theRandomlyLoadedPIPNswitchperformancedoesnot fluctuatewhentheappliedtrafficvaries.

ThethroughputoftheselectivelyloadedPIPNis expectedtobebetter thanthatoftherandomlyloaded PIPNasithasfewerstages.However,Itisshownfrom thegivenType -IIpatternsthattheselectivelyloaded PIPNisnotalwayssuperiorovertherandomlyloaded (patterns6 -19).Underheterogeneoustrafficmodels,the selectivelyloadingtechniquemayoverloadsome subnetworks,increasingthenumberofcollisions,while leavingothersubnetworkslightlyloaded.

4.Conclusions

Inthispaper,ahighperformancebanyanbasedATM switchisintroduced.Thereplicationtechni queisapplied tothePIPN.Theswitchusesthereplicationtechniqueto providemultiplepathsbetweeninputsandoutputsand usesthePIPNtosmooththeheterogeneoustrafficmodels. Theexistenceofmorepathsbetweeneachinput -output portspairsmakesthemodifiedswitchesmorereliable thantheoriginalPIPN.

Theperformanceoftwotechniquesfordistributing cellsamongthesubnetworksoftheReplicatedPIPNis examinedanalyticallyandbysimulation.Bothanalytical andsimulationresultsarecoh erent.Itisshownthatthe ReplicatedPIPNgivesbetterperformancethanthe originalPIPNundervarioustraffictypes.Buffer dimensioninganalysisisperformedtochooseasuitable buffersize.

Theanalysisshowsthatselectivelyloadingtechniqueis betterthantherandomlyloadingtechniqueunderuniform trafficmodel.Thisisduetothefewernumberofstagesin theformertechnique.However,underheterogeneous trafficmodels,therandomlyloadingtechniquebecomes betterthantheselectivelyloadin gtechniqueasthesecond techniquemayoverloadsomesubnetworkswhileother subnetworksarelightlyloadedcausingmorecontentionin theoverloadedsubnetworkswhiletherandomlyloading techniquedistributesincomingcellsequiprobablyamong thesubnetworks.

Theresultingswitchhasasignificantincreasein performanceunderhomogeneousandheterogeneous

traffic models which supports the idea of using it as a new ATMs witch.

Forfuturework, the performance of the switch can be tested under other arri valtraffic models. The implementation aspects of the switches, such as cost and reliability, may be studied in more detail.







Fig.13.Performanceunder (0.30,0.02,0.15,0.00,0.20,0.06,0.22,0.05) Type -Itrafficfordif ferentnetworksizes

Table1.Averagepercentagethroughputimprovement forreplicatedPIPNovertheoriginalPIPN

Net.Size	R ₂	S_2	R ₄	S_4
16x16	10.2	12.1	15.5	19.2
64x64	20.0	21.7	30.9	34.8
256x256	28.2	29.9	45.3	49.6

Table2.Summaryofperformanceresultsfor256x256replicatedPIPNandPIPN

Net.	PIPN	R ₂	S_2	R ₄	S ₄
Туре					
Min.	0.2571	0.4425	0.3154	0.6121	0.3914
Max.	0.3216	0.4943	0.5298	0.6452	0.6937
Avg.	0.3040	0.4823	0.4094	0.6365	0.5494
Max-Min	0.0645	0.0517	0.2143	0.0330	0.3023
Std.Dev.	0.0201	0.0156	0.0722	0.0097	0.0955

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AppendixA

HerewelistthepatternsofType -IItrafficmodelused tocomparetheperformanceofthereplic atedandoriginal PIPN[4,5].

Table 3. Throughput of 256 x 256 replicated PIPN and PIPN under various Type

-IItrafficpatterns

No	Type-IITraffic	OriginalPIPN	R ₂	S_2	R ₄	S_4
		(thr)	(thr)	(thr)	(thr)	(thr)
1	(0.12,0.13,0.25,0.50)	0.321455	0.49436	0.52983	0.64185	0.69378
2	(0.05, 0.05, 0.45, 0.45)	0.318803	0.49306	0.52803	0.64381	0.66568
3	(0.05,0.45,0.10,0.40)	0.311484	0.48618	0.51738	0.63853	0.64850
4	(0.45,0.05,0.05,0.45)	0.310813	0.48574	0.52115	0.63896	0.64041
5	(0.00,0.20,0.00,0.80)	0.319086	0.49078	0.47911	0.63695	0.63532
6	(0.45,0.05,0.40,0.10)	0.317029	0.48899	0.41857	0.64071	0.61593
7	(0.40,0.30,0.20,0.10)	0.314419	0.49033	0.41687	0.64202	0.56963
8	(0.30,0.00,0.60,0.10)	0.3175056	0.49177	0.41542	0.64265	0.59706
9	(0.50,0.25,0.15,0.10)	0.307978	0.48532	0.41593	0.64025	0.55118
10	(0.05,0.45,0.45,0.05)	0.318976	0.49070	0.38730	0.64201	0.59481
11	(0.00,0.00,0.001.00)	0.321693	0.49148	0.35410	0.63361	0.56148
12	(0.25,0.25,0.50,0.00)	0.320476	0.49418	0.35364	0.64522	0.56473
13	(0.70,0.150.10,0.05)	0.293638	0.47319	0.37188	0.63425	0.48825
14	(0.45,0.45,0.05,0.05)	0.298879	0.48488	0.38102	0.64292	0.46144
15	(0.00,0.20,0.80,0.00)	0.311829	0.49018	0.35228	0.64206	0.51480
16	(0.80,0.10,0.06,0.04)	0.284395	0.46394	0.35225	0.62463	0.46107
17	(0.00,0.00,1.000.00)	0.291829	0.48364	0.35382	0.64009	0.39243
18	(1.00,0.00,0.00,0.00)	0.257484	0.44259	0.31545	0.61262	0.39147
19	(0.00,1.00,0.00,0.00)	0.257191	0.44362	0.31572	0.61217	0.39152